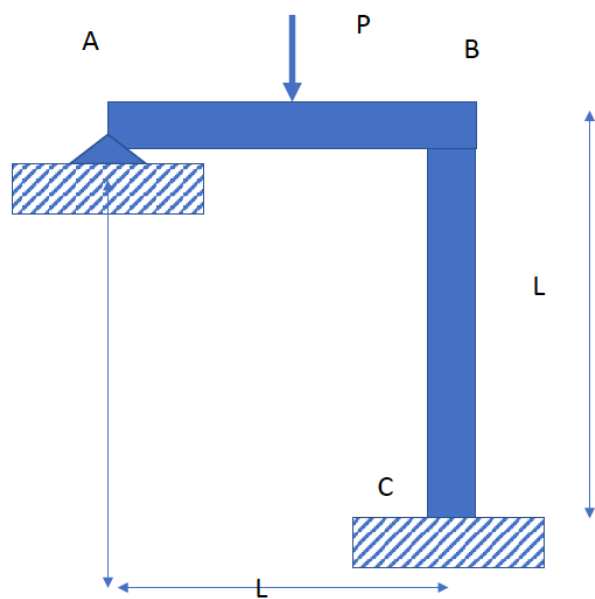
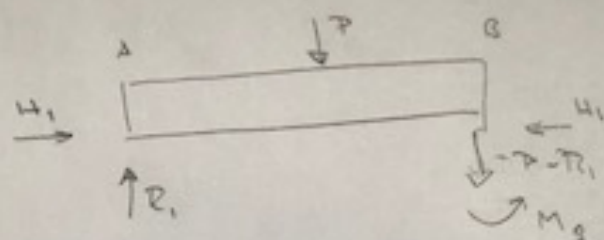




Calcular as reações em A e C





$$M_3 = R_1 L - \frac{PL}{2}$$

+ EQUILÍBRIO (GLOBAL)

$$\begin{aligned} H_1 + H_2 &= 0 \\ R_1 + R_2 - P &= 0 \\ -R_2 L + H_2 L + \frac{PL}{2} &= 0 \end{aligned}$$

└ SISTEMA ESTATICAMENTE  
NÃO DETERMINADO

$$R_1 = \frac{1}{L} \left[ H_1 L + \frac{PL}{2} \right] = H_1 + \frac{P}{2}$$

# CONDIÇÃO CINEMÁTICA

$$\left\{ \int_{\Delta} \frac{\partial U}{\partial H_2} = 0 \right\}$$

$$U = U_{AG} + U_{BC}$$

$$U_{AG} = \underbrace{\int_0^L \frac{H_1^2}{2EA} dx}_{\text{COMPRESSÃO}} + \underbrace{\int_0^L \frac{\left(\frac{P}{2} \left\langle x - \frac{L}{2} \right\rangle - R_1 x\right)^2}{2EI} dx}_{\text{FLEXÃO}}$$

$$U_{BC} = \int_0^L \frac{-(R_1 - P)^2}{2EA} dy + \int \frac{(-M_2 - H_2 y)^2}{2EI} dy$$

$$\frac{\partial U}{\partial H_1} = \frac{H_1 L}{EA} + \frac{1}{EI} \frac{\partial R_1}{\partial H_1} \left[ \frac{5PL^3}{48} - \frac{R_1 L^3}{3} \right]$$

$$+ \frac{(R_1 - P)}{EA} \frac{\partial R_1}{\partial H_1} L + \frac{1}{EI} \left[ -M_2 \frac{\partial H_2}{\partial H_1} L - H_2 \frac{\partial M_2}{\partial H_1} \frac{L^2}{2} + H_2 \frac{L^3}{2} \right]$$

$$+ \frac{H_2 L^3}{3} \Big] = 0$$

(3)

Sendo que:

$$\left\{ \frac{\partial \mathcal{R}_1}{\partial u_2} = 1 \right\} \quad \Leftrightarrow \quad \frac{\partial M_3}{\partial u_2} = \frac{\partial \mathcal{R}_1}{\partial u_2} L = L$$

$$\frac{u_1 L}{EA} + \frac{1}{EI} \left[ \frac{5PL^3}{48} - \left( u_2 + \frac{P}{2} \right) \frac{L^3}{3} \right] + \left( u_1 - \frac{P}{2} \right) \frac{1}{EA} L +$$

$$+ \frac{1}{EI} \left[ - \left( 2L - \frac{PL}{2} \right) L^2 - \cancel{u_2 \frac{L^3}{3}} + \left( 2L - \frac{PL}{2} \right) \frac{L^2}{2} + \cancel{u_1 \frac{L^3}{3}} \right] = 0$$

$$\frac{u_1 L}{EA} - \frac{1}{EI} \left[ - \frac{PL^3}{16} - \frac{u_1 L^3}{3} \right] + \left( u_1 - \frac{P}{2} \right) \frac{L}{EA} = 0$$

$$u_2 = P \frac{\left[ \frac{L^3}{16EI} - \frac{L}{2EA} \right]}{\left[ \frac{2L+1}{A} + \frac{L^3}{3EI} \right]}$$

...